Section 4

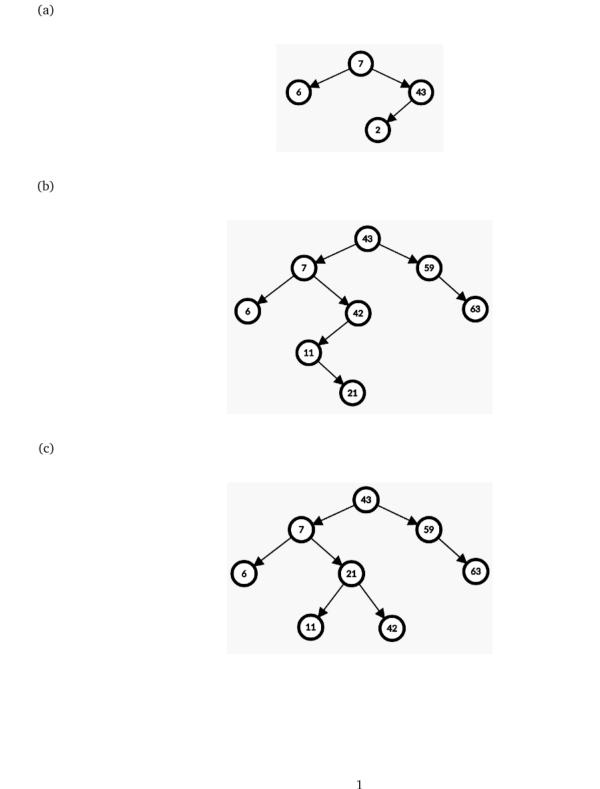
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Section 04: Midterm Review

1. Valid BSTs and AVL Trees

For each of the following trees, state whether the tree is (i) a valid BST and (ii) a valid AVL tree. Justify your answer.



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2. Hash table insertion

For each problem, insert the given elements into the described hash table. Do not worry about resizing the internal array.

(a) Suppose we have a hash table that uses separate chaining and has an internal capacity of 12. Assume that each bucket is a linked list where new elements are added to the front of the list.

Insert the following elements in the EXACT order given using the hash function h(x) = 4x: 0, 4, 7, 1, 2, 3, 6, 11, 16

(b) Suppose we have a hash table that uses linear probing and has an internal capacity of 13. Insert the following elements in the EXACT order given using the hash function h(x) = 3x:
2, 4, 6, 7, 15, 13, 19

(c) Suppose we have a hash table that uses quadratic probing and has an internal capacity of 10. Insert the following elements in the EXACT order given using the hash function h(x) = x: 0, 1, 2, 5, 15, 25, 35

(d) Suppose we have a hash table implemented using separate chaining. This hash table has an internal capacity of 10. Its buckets are implemented using a linked list where new elements are appended to the end. Do not worry about resizing.Show what this hash table internally looks like after inserting the following key-value pairs in the order given

Show what this hash table internally looks like after inserting the following key-value pairs in the order given using the hash function h(x) = x:

(1, a), (4, b), (2, c), (17, d), (12, e), (9, e), (19, f), (4, g), (8, c), (12, f)

3. Evaluating hash functions

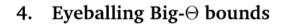
Consider the following scenarios.

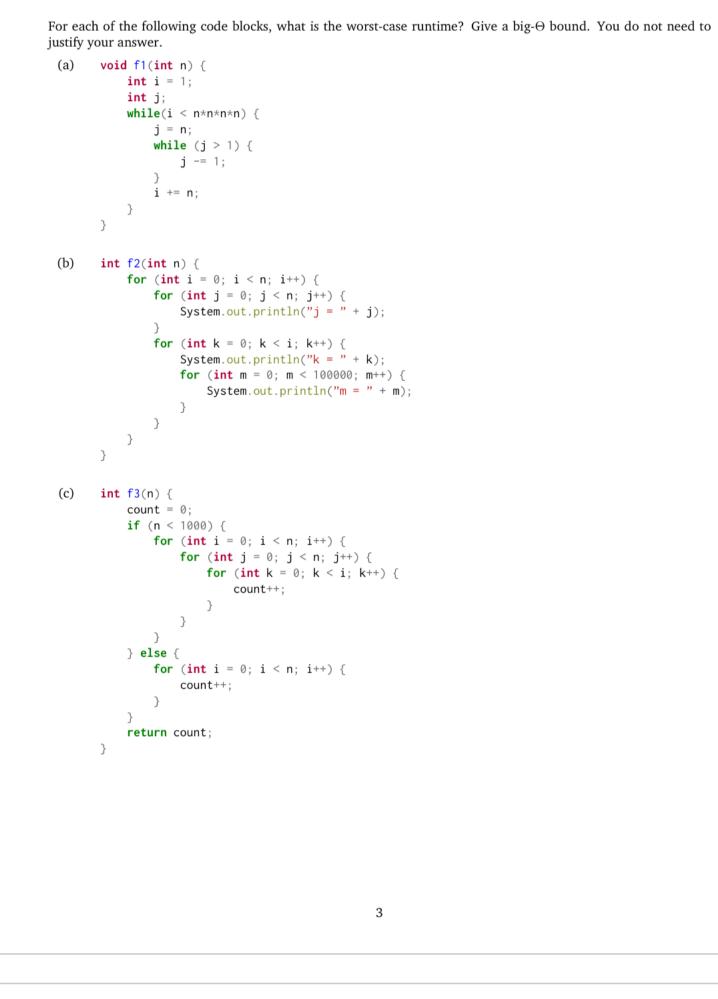
(a) Suppose we have a hash table with an initial capacity of 12. We resize the hash table by doubling the capacity. Suppose we insert integer keys into this table using the hash function h(x) = 4x.Why is this choice of hash function and initial capacity suboptimal? How can we fix it?

(b) Suppose we have a hash table with an initial capacity of 8 using quadratic probing. We resize the hash table by doubling the capacity.

Suppose we insert the integer keys 2^{20} , $2 \cdot 2^{20}$, $3 \cdot 2^{20}$, $4 \cdot 2^{20}$, ... using the hash function h(x) = x. Describe what the runtime of the dictionary operations will over time as you keep adding these keys to the table.

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(d) void f4(int n) {
 // NOTE: This is your data structure from the first project.
 LinkedDeque<Integer> deque = new LinkedDeque<>();
 for (int i = 0; i < n; i++) {
 if (deque.size() > 20) {
 deque.removeFirst();
 }
}

	<pre>deque.addLast(i);</pre>			
	<pre>(int i = 0; i < deque.size(); i++) { System.out.println(deque.get(i));</pre>			
}				

5. Best case and worst case runtimes

For the following code snippet give the big- Θ bound on the worst case runtime as well the big- Θ bound on the best case runtime, in terms of n the size of the input array.

1	<pre>void print(int[] input) {</pre>
2	int i = 0;
3	<pre>while (i < input.length - 1) {</pre>
4	if $(input[i] > input[i + 1]) $ {
5	<pre>for (int j = 0; j < input.length; j++) {</pre>
6	<pre>System.out.println("uh I don't think this is sorted plz help");</pre>
7	}
8	} else {
9	<pre>System.out.println("input[i] <= input[i + 1] is true");</pre>
10	}
11	i++;
12	}
13	}

6. Big-O, Big-Omega True/False Statements

For each of the statements determine if the statement is true or false. You do not need to justify your answer.	
(a) $n^3 + 30n^2 + 300n$ is $\mathcal{O}(n^3)$	

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(b) nlog(n) is O(log(n))

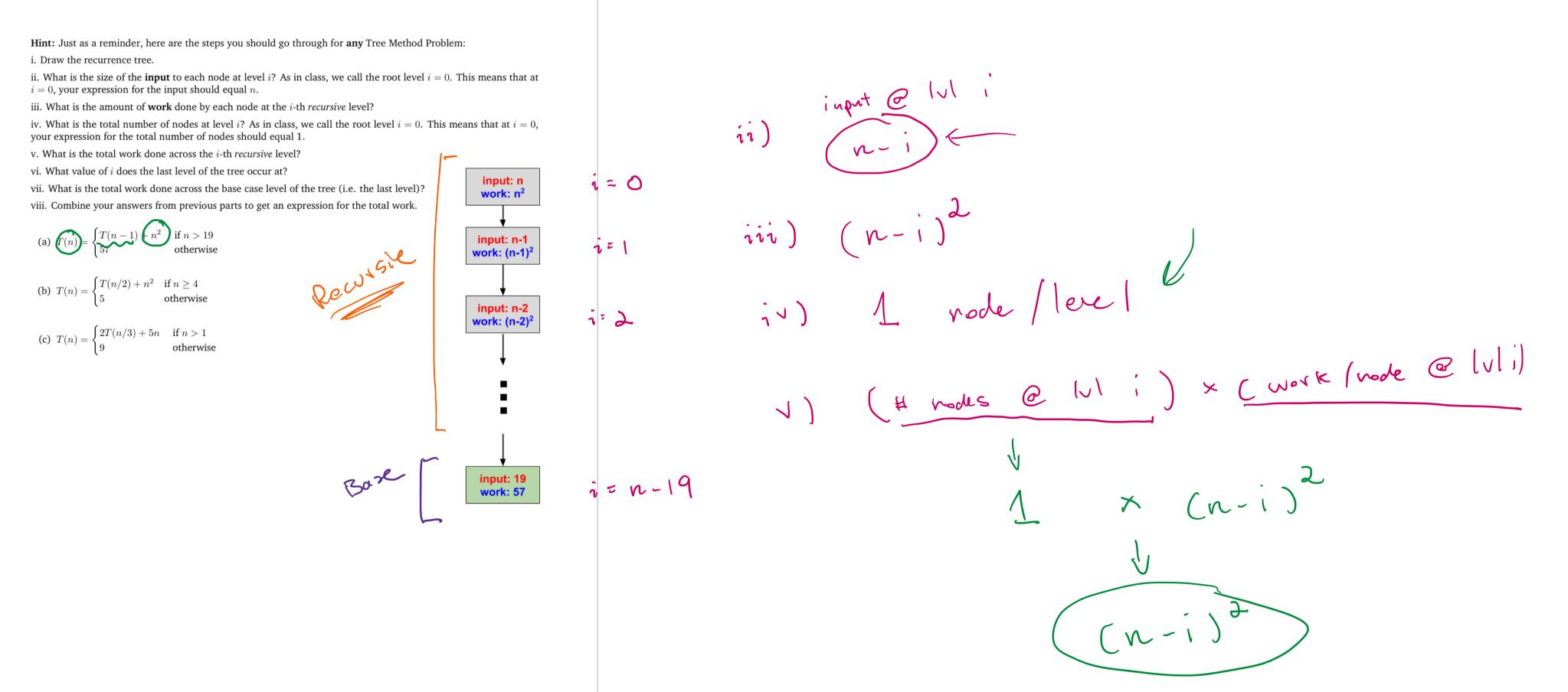
(c) $n^3 - 3n + 3n^2$ is $\mathcal{O}(n^2)$

(d) 1 is $\Omega(n)$

(e) $.5n^3$ is $\Omega(n^3)$

7. Tree Method

Find a summation for the total work of the following expressions using the Tree Method.



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VII



8. Modeling

Consider the following method. Let n be the integer value of the n parameter, and let m be the size of the Linked-Deque.

public int mystery(int n, LinkedDeque<Integer> deque) { **if** (n < 7) { System.out.println("???"); int out = 0; for (int i = 0; i < n; i++) { out += i; return out; } else { System.out.println("???"); System.out.println("???"); out = 0; // NOTE: Assume LinkedDeque has working, efficient iterator. for (int i : deque) { out += 1; for (int j = 0; j < deque.size(); j++) {</pre> System.out.println(deque.get(j)); return out + 2 * mystery(n - 4, deque) + 3 * mystery(n / 2, deque);

} Give a recurrence formula for the **worst-case** running time of this code. It's OK to provide a O for non-recursive terms (for example if the running time is A(n) = 4A(n/3) + 25n, you need to get the 4 and the 3 right but you don't have to worry about getting the 25 right). Just show us how you got there.

9. Hash tables

}

(a) Consider the following key-value pairs.

(6, a), (29, b), (41, d). (34, e), (10, f), (64, g), (50, h)
Suppose each key has a hash function h(k) = 2k. So, the key 6 would have a hash code of 12. Insert each key-value pair into the following hash tables and draw what their internal state looks like:
(i) A hash table that uses separate chaining. The table has an internal capacity of 10. Assume each bucket

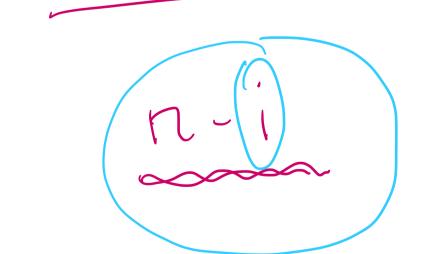
is a linked list, where new pairs are appended to the end. Do not worry about resizing. (ii) A hash table that uses linear probing, with internal capacity 10. Do not worry about resizing.

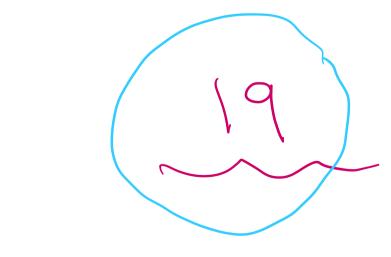
(iii) A hash table that uses quadratic probing, with internal capacity 10. Do not worry about resizing.

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input @ level 1







n-i = 19 n-19=z

Work (vore @ 6(c) nodes Ħ Θ blc X

×

- r 5

blC

-U

2 (n-i)



Base

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Recursile